

**Paper 1, TDC Part-1**  
**Chapter– 3, Mesh and Node Analysis**

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# Mesh and Nodal Analysis in Passive Circuits

Problems on Mesh Analysis with current source and super mesh.

In the earlier classes we have looked few examples of Mesh analysis with voltage sources only.

In today's lecture we will discuss the problem of circuit theory base on ~~of~~ mesh analysis with ~~a~~ current sources or sources.

To ~~solve~~ analyze the circuit with current source using mesh analysis, there are two possible methods. First, we could assign an unknown voltage across the current source, then applying KVL around each



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methods. First, unknown voltage across the current source, then applying KVL around each mesh as before and then ~~write~~ writing down the KVL eqn. for each of the meshes. This is generally more difficult approach.

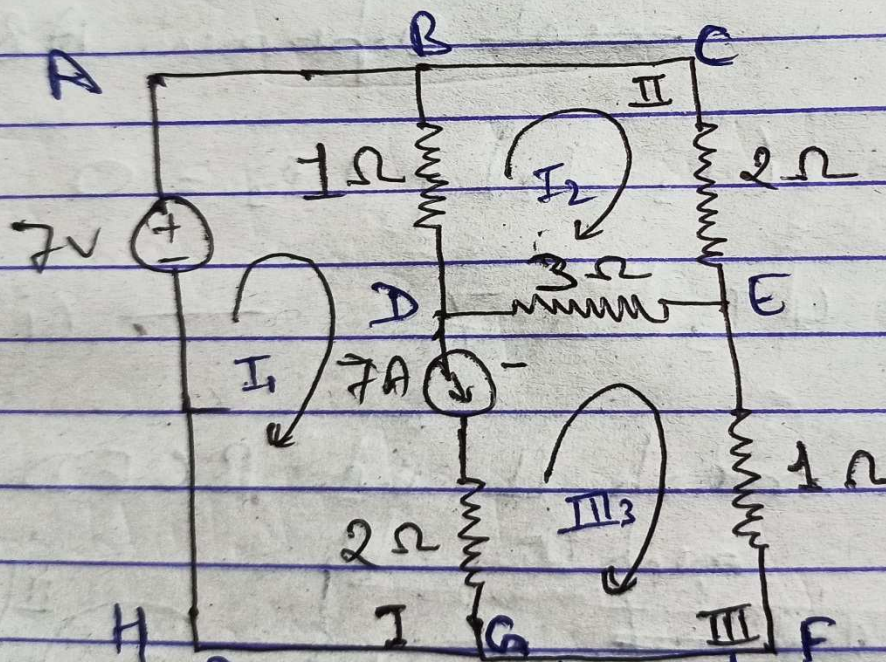
A better approach is to create a kind of "Supermesh" from the two meshes that have a current source as a common element; the current source is in the interior of the supermesh. We thus reduce the number of meshes by 1 for each current source present. If the current source lies on the perimeter of the circuit, then the single mesh in which



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It is found is ignored. KVL is then applied to only to those meshes or supermeshes in the reinterpreted network.

Ex-1) Determine the three mesh currents in below ckt. shown



Since 7A independent source is there.



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Soln: Note → Since 7A independent source is there, If we solve this problem by directly applying KVL in each of the 3 meshes I, II & III as shown above then it becomes difficult approach due to current source.

So we solve the above problem by taking supermesh whose interior is that of meshes I and III as shown below, named as A B D E F G H A.

As shown below,

The circuit diagram shows three meshes labeled I, II, and III. Mesh I is on the left, containing a 7A DC current source pointing upwards. Mesh II is in the middle, containing a 12Ω resistor. Mesh III is on the right, containing a 3Ω resistor and a 1Ω resistor in series. The nodes are labeled: A (top-left), B (top-middle), C (top-right), D (middle-left), E (middle-right), F (bottom-right), G (bottom-middle), and H (bottom-left). A dashed line indicates a supermesh formed by meshes I and III, bypassing the 12Ω resistor in mesh II. Currents  $I_1$ ,  $I_2$ , and  $I_3$  are indicated for meshes I, II, and III respectively.



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Current through  $1\Omega$  resistor of branch BD is  $(I_1 - I_2)$ . Similarly current through  $3\Omega$  resistor of branch DE is  $(I_3 - I_2)$  and current through  $1\Omega$  resistor of branch EF is  $I_3$ .

Applying KVL in ~~mesh~~ supermesh ABDEFGHA

$$-7 + 1(I_1 - I_2) + 3(I_3 - I_2) + 1I_3 = 0$$

$$\text{or } I_1 - 4I_2 + 4I_3 = 7 \quad \text{--- (i)}$$



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Applying KVL in mesh II i.e. B C E D B

Applying KVL in this ~~loop~~ <sup>mesh II</sup>

$$-2I_2 + 3(I_2 - I_3) + 1(I_2 - I_1) = 0$$

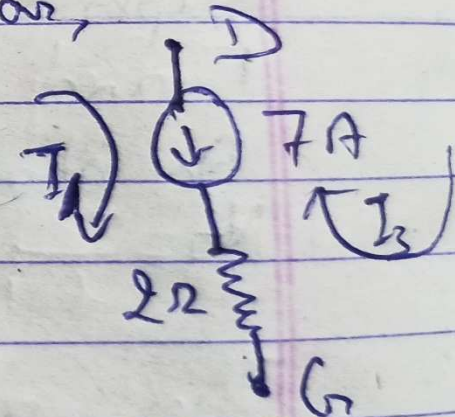
$$-I_1 + 6I_2 - 3I_3 = 0$$

$$\text{or } I_1 - 6I_2 + 3I_3 = 0 \quad \text{--- (ii)}$$

As we can relate the independent source current of 7A of branch D G or,

$$I_1 - I_3 = 7$$

$$\text{or } I_1 = 7 + I_3 \quad \text{--- (iii)}$$





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From eqn. (iii) putting value of  $I_1$  in eqn. (i) & (ii)

$$7 + I_3 - 4I_2 + 4I_3 = 7 \quad \text{--- (i)}$$

$$-4I_2 + 5I_3 = 0 \quad \text{--- (iv)}$$

and eqn. (ii) can be written as,

$$7 + I_3 - 6I_2 + 3I_3 = 0 \quad \text{--- (ii)}$$

$$-6I_2 + 4I_3 = -7 \quad \text{--- (v)}$$

Now  $3 \times \text{eqn. (iv)} - 2 \times \text{eqn. (v)}$  results as,

$$-12I_2 + 15I_3 = 0$$

$$+ \cancel{-12I_2} + 8I_3 = \cancel{-14}$$

$$7I_3 = 14 \Rightarrow I_3 = 2 \text{ A}$$



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$$7I_3 = 14 \Rightarrow I_3 = 2 \text{ A} //$$

$$I_1 = 7 + I_3 = (7 + 2) \text{ A} \\ = 9 \text{ A} //$$

$$\text{and } -4I_2 + 5 \times 2 = 0$$

$$4I_2 = 10 \Rightarrow I_2 = 2.5 \text{ A} //$$

~~Q~~ ~~on solve~~ The three mesh current are,

$$I_1 = 9 \text{ A}, \quad I_2 = 2.5 \text{ A}, \quad \& \quad I_3 = 2 \text{ A}.$$

Hence using supermesh method we solve the problem easily. But it was difficult to solve the

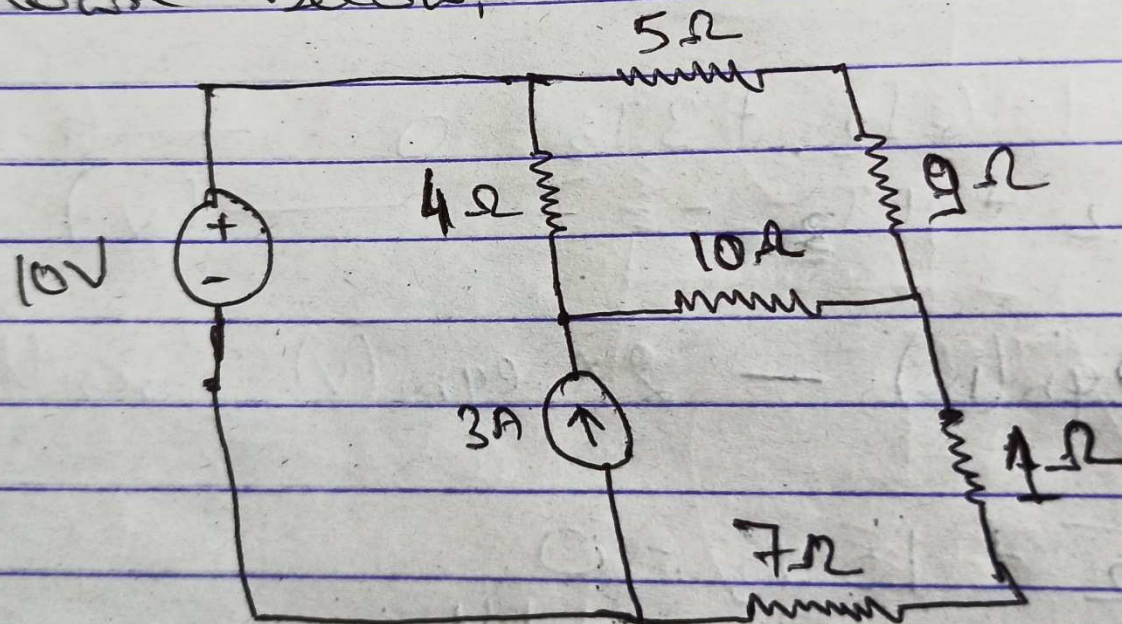


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problem if we apply the mesh KVL to all the 3 loops I, II & III.

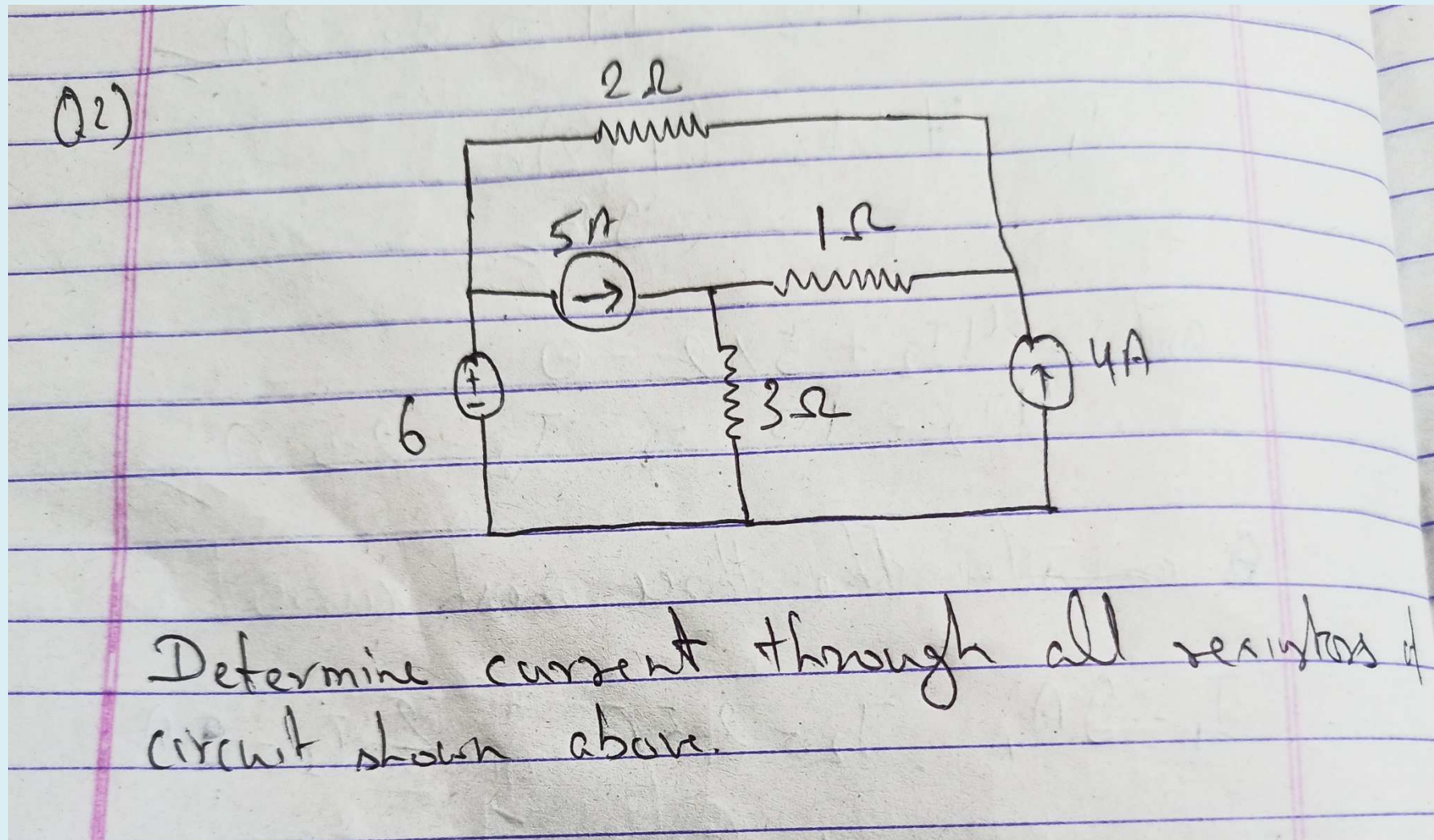
Question for practice

Q Determine the current  $i_x$  in the circuit shown below,





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For any query contact- 9771474020

**Thank You**