

Paper 1, TDC Part-1
Chapter– 3, Mesh and Node Analysis
Solution of problems

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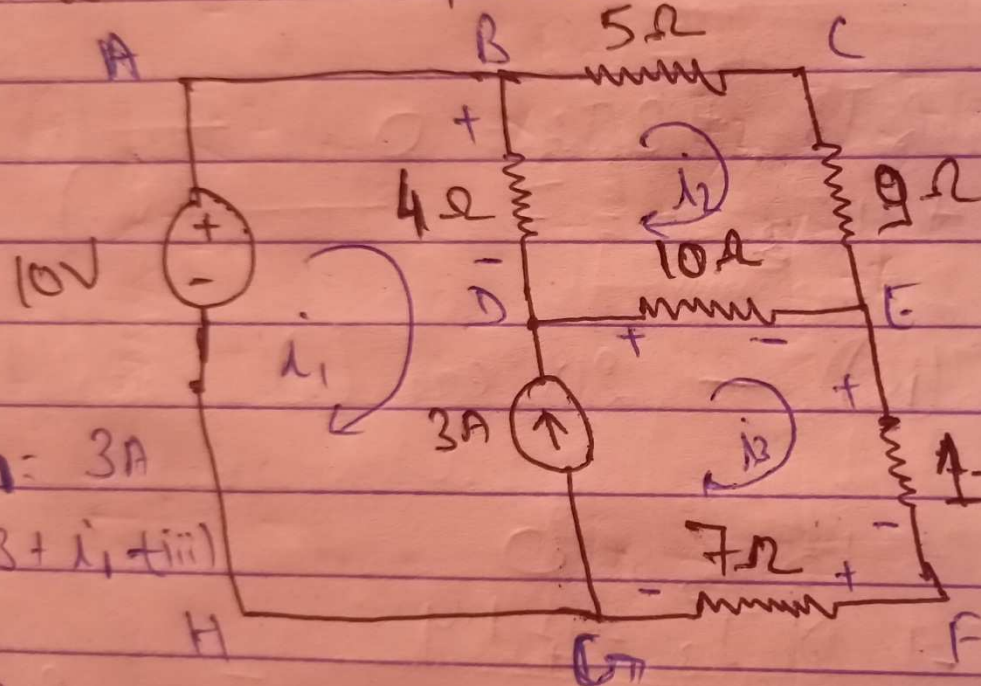
L.S. College, BRA Bihar University,

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Mesh and Nodal Analysis in Passive Circuits

Question for practice

Determine the current i_1 in the circuit shown below,



2 supernodes AB DE FGH
 $4i_1 - 14i_2 + 18i_3 = 10 - 10$

In mesh BCEDB
 $+4i_1 - 28i_2 + 10i_3 = 0$

$22i_1 - 14i_2 = -44 \times 2$

$14i_1 - 28i_2 = -30$

$30i_1 - 58i_2 = 0$

$i_1 = \frac{-58}{30} \times \frac{-29}{15} = 1.07 \text{ A}$

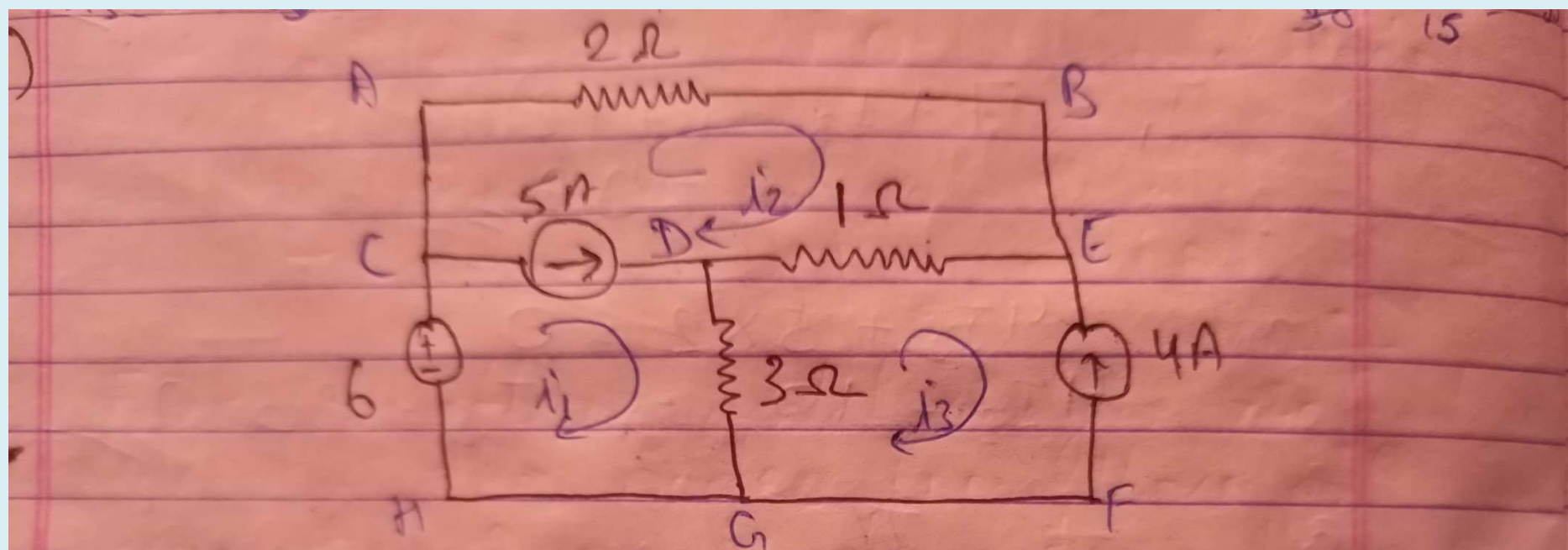
$i_3 - i_2 = 3 \text{ A}$

$i_3 = 3 + i_2$

$i_3 = 3 - 1.93 \text{ A} = 1.07 \text{ A}$

$i_2 = 0.11 \text{ A}$

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Determine current through all resistors of circuit shown above.

$$i_3 = -4A$$

$$i_1 - i_2 = 5A$$

$$i_1 = 5 + i_2$$

In supermesh ABEDGHA

$$3i_1 + 3i_2 - 4i_3 = 6$$

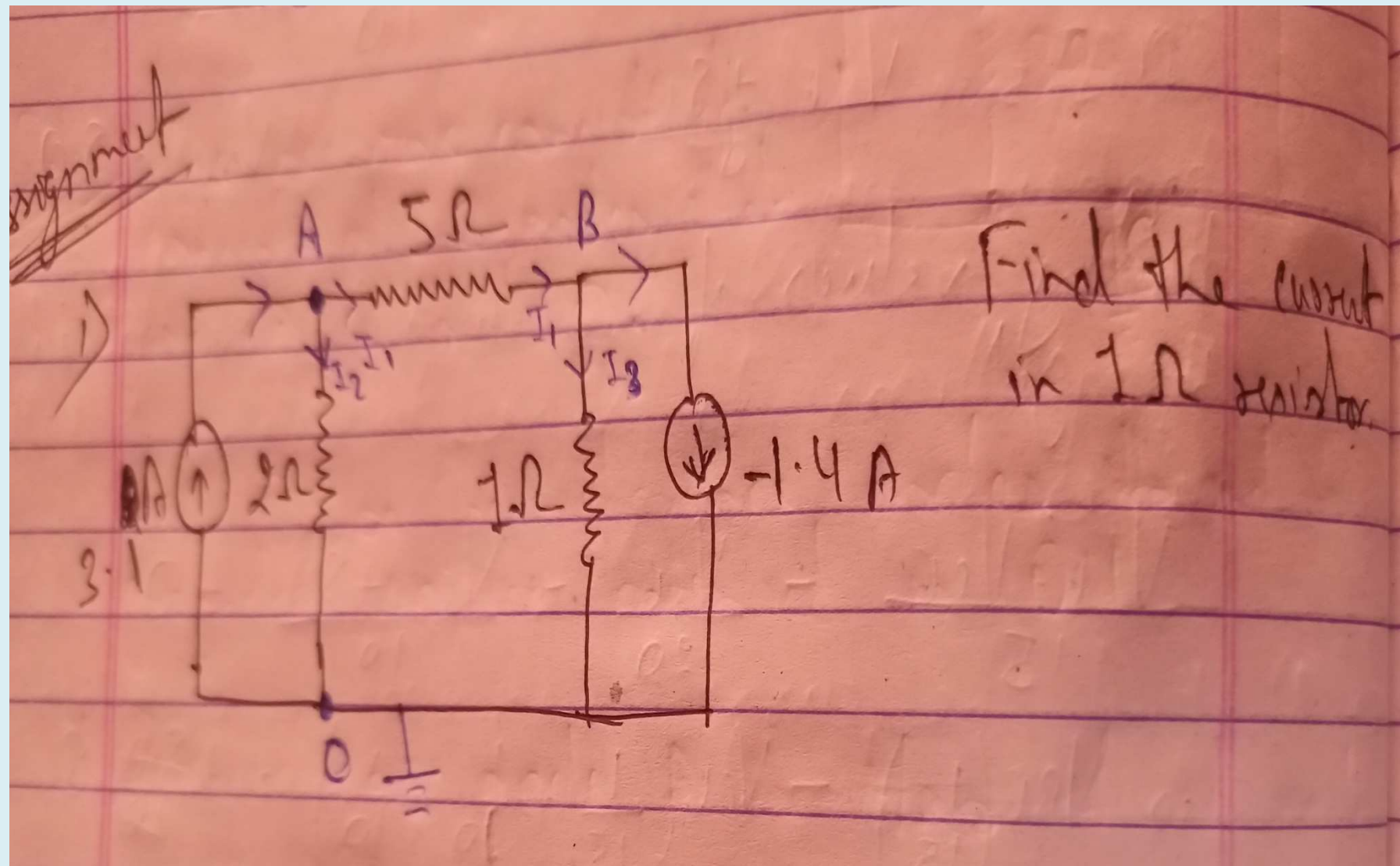
$$3(5 + i_2) + 3i_2 - 4(-4) = 6$$

$$6i_2 + 31 = 6$$

$$i_2 = \frac{-25}{6} = -4.17A$$

$$i_1 = 5 - 4.17 = .83A$$

Mesh and Nodal Analysis in Passive Circuits



Mesh and Nodal Analysis in Passive Circuits

Ex: 1) We have node A, B and O i.e. $n=3$ let reference node is O, then ~~V_{AO}~~ at node A voltage is V_{AO} & at node B voltage is V_{BO} , and as reference node O is grounded then there is voltage '0'.

Now applying KCL at node A,

$$3.1 = I_1 - I_2 = 0$$

$$I_1 + I_2 = 3.1$$

$$\frac{V_{AB}}{5} + \frac{V_{AO}}{2} = 3.1 \Rightarrow \frac{V_{AO} - V_{BO}}{5} + \frac{V_{AO}}{2} = 3.1$$

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$$\frac{7V_{A0}}{10} - \frac{V_{B0}}{5} = 3.1 \Rightarrow 7V_{A0} - 2V_{B0} = 31 \quad (i)$$

KCL at node B, $I_1 - I_3 - (-1.4A) = 0$

$$I_1 - I_3 + 1.4 = 0$$

$$\Rightarrow \frac{V_{A0}}{5} - \frac{V_{B0}}{1} = -1.4$$

$$\Rightarrow \frac{V_{A0}}{5} - \frac{6V_{B0}}{5} = -1.4 \Rightarrow V_{A0} - 6V_{B0} = -7 \quad (ii)$$

eqn (i) ~~x3~~ = eqn. (ii) results

$$21V_{A0} - 6V_{B0} = 93$$

$$-V_{A0} + \cancel{6V_{B0}} = +7$$

$$20V_{A0} = 100 \Rightarrow V_{A0} = \frac{100}{20} = 5V$$

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$$V_{BO} = \frac{31 - 35}{-2} = \frac{+4}{+2} = 2V$$

Current flowing ~~left to right~~ through the 1Ω resistor is

$$I_{1\Omega} = \frac{V_{BO}}{1\Omega} = \frac{2V}{1\Omega} = 2A$$

$$\text{or, } I_1 = I_3 + (-1.4)$$

$$\text{or, } I_3 = I_1 + 1.4$$

$$I_3 = \frac{V_{AO} - V_{BO}}{5} + 1.4$$

$$= \frac{5 - 2}{5} + 1.4 = \frac{3}{5} + 1.4 = 0.6 + 1.4 = 2A$$

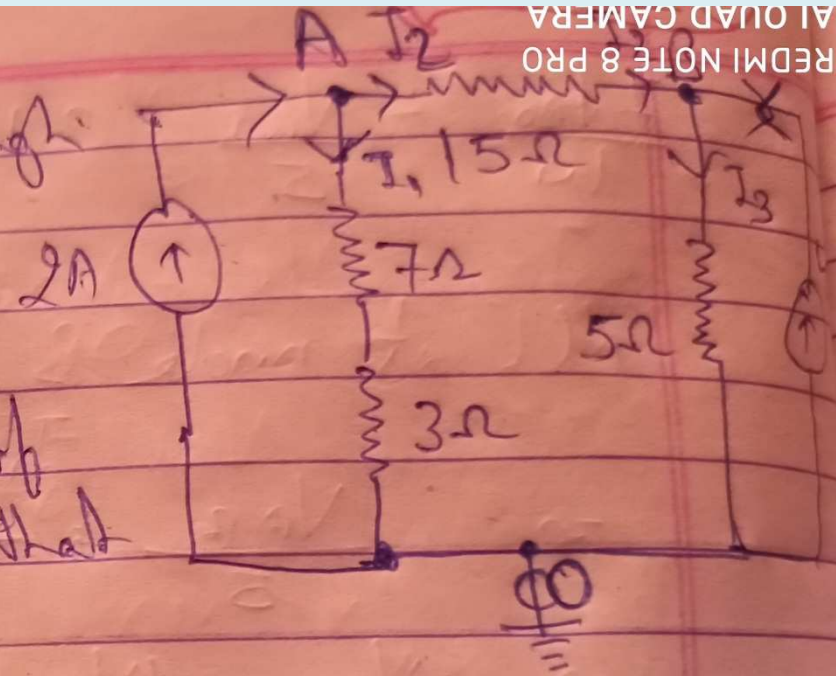
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(2) To find current through 15Ω resistor from left to right.

Soln The network consist of consist of 3 nodes that are A, B and O.

Let O be the reference nodes ~~that~~ and is grounded so its potential is 0V.

Let Potential at node A is V_{AO} & at node B is V_{BO} ,



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Applying KCL at node A.

$$2A + I_1 - I_2 = 0$$

$$\text{or } I_1 + I_2 = 2$$

$$\frac{V_{AO}}{(7+3)} + \frac{V_{AB}}{15} = 2$$

$$\Rightarrow \frac{V_{AO}}{10} + \frac{V_{AO} - V_{BO}}{15} = 2$$

$$\Rightarrow \frac{5V_{AO} - 2V_{BO}}{30} = 2$$

$$\text{or } 5V_{AO} - 2V_{BO} = 60 \text{ ————— (i)}$$

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KCL at node B,

$$I_2 + 4A = I_3$$

$$I_3 - I_2 = 4A$$

$$\frac{V_{B0}}{5} + \frac{V_{A0} - V_{B0}}{15} = 4$$

$$\Rightarrow V_{A0} + 2V_{B0} = 60 \quad \text{--- (ii)}$$

Adding eqn. (i) & (ii) results

$$6V_{A0} = 120 \Rightarrow V_{A0} = 20V$$

$$V_{B0} = 20V$$

$$\begin{aligned} \text{Current in } 15\Omega \text{ resistor is } I_{15\Omega} &= \frac{V_{AB}}{15} \\ &= \frac{V_{A0} - V_{B0}}{15} = \frac{20 - 20}{15} = 0 \end{aligned}$$

So current through 15Ω resistor is $0A$.

Mesh and Nodal Analysis in Passive Circuits

For any query contact- 9771474020

Thank You