

# **Paper 1, TDC Part-1 Problem Discussion**

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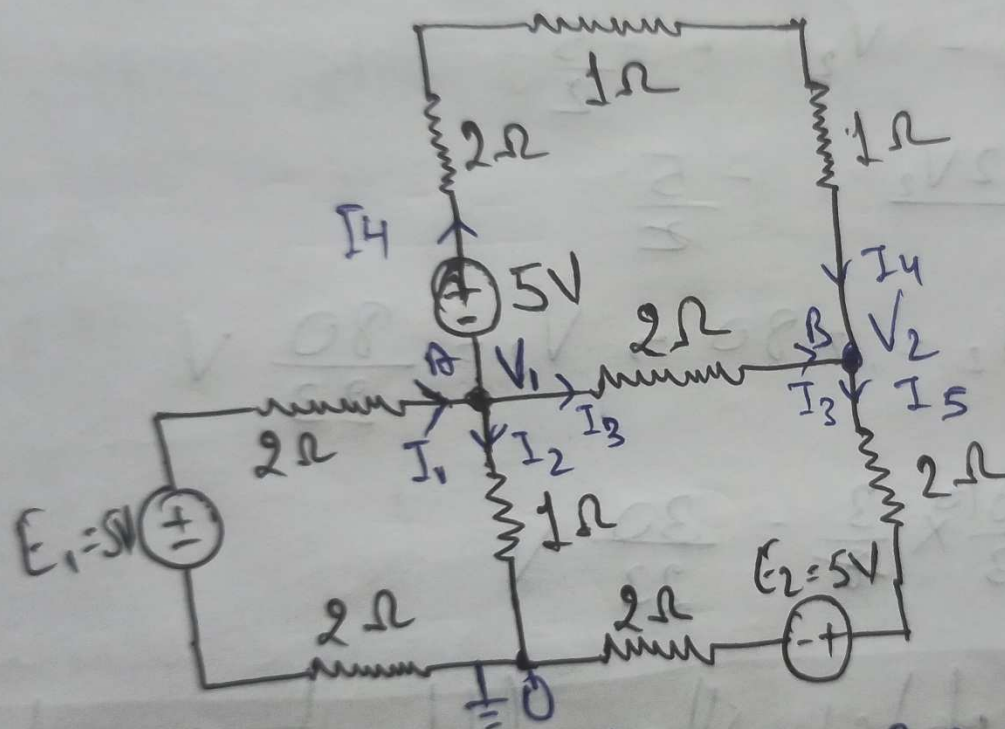
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# Mesh and Nodal Analysis in Passive Circuits

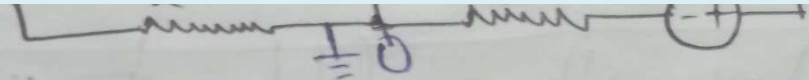
Q1) Using Nodal Method, find the battery current in the circuit shown below.



Soln.

There are 3 nodes A, B, & 0 where 0 is reference node and is grounded. Let voltages at A and B be  $V_1$  &  $V_2$  resp.

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There are 3 nodes A, B, & 0 where 0 is reference node and is grounded. Let voltages at A & B are  $V_1$  &  $V_2$  resp.

Also let different branch currents are  $I_1, I_2, I_3, I_4$  &  $I_5$  as shown in figure.

Then applying KCL at node A, we have

$$I_1 = I_2 + I_3 + I_4$$
$$\text{or, } \frac{E_1 - V_1}{4} = \frac{V_1}{2} + \frac{V_1 - V_2}{2} + \frac{V_1 + 5 - V_2}{4}$$
$$\text{or, } \frac{5}{4} = V_1 \left( \frac{1}{4} + \frac{1}{4} + \frac{1}{2} + 1 \right) - V_2 \left( \frac{1}{2} + \frac{1}{4} \right) + \frac{5}{4}$$
$$\text{or, } 0 = 2V_1 - \frac{3}{4}V_2 \Rightarrow 8V_1 - 3V_2 = 0$$
$$\text{or, } V_1 = \frac{3}{8}V_2$$

## Mesh and Nodal Analysis in Passive Circuits

Now applying KCL at node B, we have

$$I_3 + I_4 = I_5$$

$$\frac{V_1 - V_2}{2} + \frac{V_1 + 5 - V_2}{4} = \frac{V_2 - 5}{4}$$

$$\text{or } V_1 \left( \frac{1}{2} + \frac{1}{4} \right) - V_2 \left( \frac{1}{2} + \frac{1}{4} + \frac{1}{4} \right) = -\frac{5}{4} - \frac{5}{4} = -\frac{5}{2}$$

$$\text{or } \frac{3}{4} V_1 - V_2 = -\frac{5}{2}$$

$$\text{or } \frac{3}{4} \times \frac{3}{8} V_2 - V_2 = -\frac{5}{2}$$

$$\text{or } \frac{9V_2 - 32V_2}{32 \cdot 16} = -\frac{5}{2}$$

$$\text{or } -23V_2 = -80 \Rightarrow V_2 = \frac{80}{23} \text{ V}$$



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$$V_1 = \frac{80}{23} \times \frac{3}{8} = \frac{30}{23} \text{ V}$$

So, we can obtain the different current now,

$$I_1 = \frac{5 - 30/23}{4} = 0.92 \text{ A}$$

$$I_2 = \frac{V_2}{1} = \frac{80}{23} \text{ A} = 3.5 \text{ A}$$

$$I_3 = \frac{\frac{30}{23} - \frac{80}{23}}{2} = \frac{-50}{46} \approx -1.0 \text{ A}$$

$$I_4 = I_1 + I_2 - I_3 = 0.92 + 1 - 3.5 = -1.58 \text{ A}$$

$$I_5 = \frac{\frac{80}{23} - 5}{4} = \frac{-1.52}{4} = -0.38 \text{ A}$$

## Mesh and Nodal Analysis in Passive Circuits

Two wires A and B are connected in series at  $0^\circ\text{C}$  and resistance of B is 3.5 times that of A. The resistance temperature co-efficient of A is  $0.4\%$  and that of the combination is  $0.1\%$ . Find the resistance temperature co-efficient of B.

$$\frac{R_B}{R_A} = 3.5 \quad \text{--- (i)}$$

# Mesh and Nodal Analysis in Passive Circuits

As per ratio 4 proportion

$$\begin{array}{c}
 \frac{A}{0.004} \quad \quad \quad \frac{B}{\alpha_B} \\
 \quad \quad \quad \swarrow \quad \searrow \\
 \quad \quad \quad 0.001 \\
 \quad \quad \quad \swarrow \quad \searrow \\
 (0.001 - \alpha_B) \quad \quad \quad 0.003
 \end{array}$$

$$\Rightarrow \frac{R_B}{R_A} = \frac{0.003}{(0.001 - \alpha_B)}$$

$$\text{or, } 3.5 = \frac{0.003}{(0.001 - \alpha_B)}$$

$$\text{or, } 3.5 \times 10^{-3} - 3.5 \alpha_B = 3 \times 10^{-3}$$

$$\text{or, } 3.5 \alpha_B = (3.5 - 3) \times 10^{-3}$$

$$\alpha_B = \frac{0.5}{3.5} \times 10^{-3}$$

$$= 0.00014^\circ \text{C}^{-1}$$

$$= 0.014\%$$

# **Mesh and Nodal Analysis in Passive Circuits**

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**Thank You**